On the LearnAbility of Abstraction Theories from Observations for Relational Learning

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Abstract. The most common methodology in symbolic learning consists in inducing, given a set of observations, a general concept definition. It is widely known that the choice of the right description language for a learning problem can affect the efficacy and effectiveness of the learning task. Furthermore, most of the real-world domain are contaminated by various kinds of imperfections in data such as inappropriateness of the description language which does not contain/facilitate an exact representation of the target concept. To deal with such kind of situations, Machine Learning approaches have moving from a framework exploiting a single inference mechanism, such as induction, towards one integrating multiple inference strategies such as abstraction. The literature so far assumed that the information needed to the learning systems to apply additional inference strategies is provided by the an expert domain. The objective in this work is the automatic inference of such information.
The efficacy of the proposed method in generating effective theories to perform abstraction was tested by providing the generated abstraction theories to the learning system INTHELEX allowing it to exploit its multistrategy capabilities, in particular the abstraction one. Various experiments were carried out on a real-world application domain of scientific paper documents showing the validity of the proposed method.

1 Introduction

The efficacy of induction algorithms has been demonstrated on a wide variety of benchmark domains. However, current machine learning techniques are inadequate for learning in more difficult real-world domains like weather prediction, financial risk analysis and drug design. The nature of the problem can be of different type as noise in the descriptions and lack of data, but also the low level representation of the examples of the target concept. It is well known that the inappropriateness of the description language, which does not contain/facilitate an exact representation of the target concept, can affect the efficacy/effectiveness of the learning task. Hence, the choice of the right representation for a learning problem has a significant impact on the performance, in general, of Machine Learning systems and, in particular of ILP systems [10]. Generally, a low level representation is made up of all the information necessary to the learning task, but individual parts contained in the representation are only remotely related to

the target concept, making pattern hard to identify. Low level representations are common in real-world domains, where examples are naturally described by many small measurements, in which there is not enough knowledge in order to represent the data in few highly relevant features.

Various strategies have been proposed to overcome this limitation, like as the different ways to exploit the framework for the *abstraction* strategy proposed in [15]. In [16], for example, the abstraction is exploited to address the problem of potentially many mappings that can be between descriptions in first order representation language to select one particular type of mapping at a time and use it as a basis to define a new hypothesis space, performing, in this way, a *representation change*. It was also used to overcome the knowledge acquisition bottleneck that limits the learning task in particular application domains such as the automation of cartographic generalization in [11]. More generally, the abstraction is used to model *a priori* the hypothesis space before the learning process starts introducing it as a multi-strategy capability that could shift to a higher language bias when the current one does not allow to capture the target predicate definition [3, 6, 8]. From an operational viewpoint, it should deal with cases when learning can be more effective if it can take place at multiple (different) levels of complexity, which can be compared to the language bias shift considered in [2]; a useful perspective for the integration of this inference operator in an inductive learning framework was given in [15]. According to such a framework, the abstraction operator was endowed in the learning system INTHELEX [4] making it able to perform the shift.

In the current practice, it is in charge of the human expert to specify all the information needed by such strategy for being applicable. It goes without saying that quality, correctness and completeness in the formalization of such information is a critical issue, that can determine the very feasibility of the learning process. Providing it is a very difficult task because of it requires a deep knowledge of the application domain, and is in any case an error-prone activity, since omissions and errors may take place. For instance, the domain and/or the language used to represent it might be unknown to the experimenter, because he is just in charge of properly setting and running the learning system on a dataset provided by third parties and/or generated by other people. In any case, it is often not easy for non-experts to single out and formally express such knowledge in the form needed by the automatic systems, just because they are not familiar with the representation language and the related technical issues.

These considerations would make it highly desirable to develop procedures that can automatically generate such information. This work aims at proposing solutions to automatically infer the information required by the abstraction framework from the same observations that are input to the inductive process, assuming that they are sufficiently significant, and at assessing the validity and performance of the corresponding procedures. In the following of the paper, after an introduction to the general operational framework for abstraction, the method for the automatic definition of appropriate rules to fire the operator will be presented along with an experimental session on a real-world domain.

2 Abstraction Inference Strategy: The general framework

Abstraction is defined as a mapping between representations that are related to the same reference set but contain less detail (typically, only the information that is relevant to the achievement of the goal is maintained). It is useful in inductive learning when the current language bias proves not to be expressive enough for representing concept descriptions that can explain the examples. Indeed, Abstraction should be included for dealing with cases when learning can be more effective if it can take place at multiple different levels of complexity, which can be compared to the language bias shift considered in [2].

Definition 1. *Given two clausal theories T (*ground theory*) and T' (*abstract theory*) built upon different languages $\mathcal{L}$ and $\mathcal{L}'$ (and derivation rules), an* abstraction *is a triple (T, T', f), where f is a computable total mapping between clauses in $\mathcal{L}$ and those in $\mathcal{L}'$.*

An Abstraction Theory (an operational representation of f) is used to perform such a *shift of language bias* [14, 2] to a higher level representation:

Definition 2. *An* abstraction theory *from $\mathcal{L}$ to $\mathcal{L}'$ is a consistent set of clauses $c : -d_1, \ldots, d_m$ where c is a literal built on predicates in $\mathcal{L}'$, and $d_j,\ j = 1, \ldots, m$ are literals built on predicates of $\mathcal{L}$.*

i.e., it is a collection of intermediate concepts represented as a disjunction of alternative definitions.

Inverse resolution operators [10], by tracking back resolution steps, can suggest new salient properties and relations of the learning domain. Inverse resolution operators can be a valuable mechanism to build abstraction theories, as introduced in [7]. To this purpose, the absorption, inter-construction and intra-construction operators can be exploited, also in the case of first order clauses. In this work we are interested in the case of a Datalog program [1, 9] as ground space of the abstraction, as in [12], where clauses are *flattened*, hence function-free.

Definition 3 (Absorption & Inter-construction).

absorption: *let C and D be two Datalog clauses. If there exists a unifier θ such that $\exists S \subset body(C),\ S = body(D)\theta$, then applying the absorption operator yields the new clause C' such that:*
- *$head(C') = head(C)$*
- *$body(C') = (body(C) \setminus S) \cup \{head(D)\theta\}$,*

i.e., if all conditions in D are verified in the body of C, the corresponding literals are eliminated and replaced by $head(D)$.

inter-construction: *let $C = \{C_i | i = 1, \ldots, n\}$ be a set of Datalog clauses. If there exists a set of literals R and a unifier θ_i for each clause C_i, such that $\exists S_i \subset body(C_i),\ S_i = R\theta_i$, then we define:*
- *a new predicate $L \leftarrow R$*
- *for all $i = 1, \ldots, n$ $body(C_i)$ can be rewritten as $(body(C_i) \setminus S_i) \cup \{L\theta_i\}$.*

i.e., if all conditions in R are verified in the body of each $C_i \in C$, the corresponding literals are eliminated and replaced by L that is a new predicate, with a definition in the theory, never present in the description language.

A useful perspective for the integration of this inference operator in an inductive learning framework was given in [15]. In this view, concept representation deals with entities belonging to three different levels. Underlying any source of experience there is the *world*, where *concrete* objects (the 'real things') reside. It is not directly known, since any observer's access to it is mediated by his *perception* of it ($P(W)$). The percept reality consists in the 'physical' stimuli produced on the observer. To be available over time, these stimuli must be memorized in an organized *structure* (S), i.e. an *extensional* representation of the perceived world, in which stimuli related to each other are stored together. Finally, to reason about the perceived world and communicate with other agents, a *language* (L) is needed, that describes it *intensionally*. World, representation and language make up a *reasoning context*. Given a reasoning context, it is possible to reason at any of the given levels. Indeed, moving from the perception level $P(W)$ by means of a set of operators one can propagate to higher levels, i.e. S and L, where it is possible to identify operators corresponding to the previous ones. Generally these sets contain operators for performing operations such as: grouping indistinguishable objects into equivalence classes; grouping a set of ground objects to form a new compound object[1] that replaces them in the abstract world; ignoring terms that can be in the abstract world, where they disappear; merging a subset of values that are considered indistinguishable; dropping a subset of arguments, thus reducing the arity of a relation; eliminating *all* arguments, so that the relation moves from a predicate logic to a propositional logic setting (which corresponds to a *propositional abstraction* at the language level).

3 Learning Abstraction Theories

As already pointed out, the exploitation of the Abstraction framework reported above and its integration in an inductive concept learning framework is based on the assumption that the knowledge needed to use it is provided by an expert of the application domain. In this Section we propose an approach to automatically learn such knowledge to be exploited by the abstraction operators.

The abstraction procedure reported in Section 2, aims at discarding or hiding the information that is insignificant to the achievement of the goal. In order to make the system able to perform an abstraction during the learning task, it must be provided with the operators encoding such a strategy by means of an abstraction theory for a specific application domain. An abstraction, according to Definition 1, is a tuple made up of a function f that is a computable mapping between theories built upon two different representation languages $\mathcal{L}$

[1] It is called term construction [8], and offers the most significant promises for limiting the complexity of learning in a first order logic setting, since it simplifies the matching process between hypotheses and examples.

Algorithm 1 Identification of domain rules for Abstraction Operators

Require: $\mathcal{E}^+$: set of positive observations; $\mathcal{E}^-$: set of negative observations; e: seed;
  if $\exists$ unary predicates in e **then**
    $S := \emptyset$, $UnaryPreds :=$ set of unary predicates in e
    $C := \{c_1, c_2, \ldots, c_n\}$ set of constants in the description of e
    for all $c_i \in C$ **do**
      $S_i := \{l_i \in UnaryPreds$ s.t. c_i is argument of $l_i\}$
      if ($\mid S_i \mid \neq 0$ and $\mid S_i \mid \neq 1$) **then** $S := S \bigcup S_i$
    for i=1..n **do**
      for all $S_j \in S$ **do**
        find all the subsets s_{jm} of S_j s.t.
          $(0 - \alpha \leq Score(s_{jm}) \leq 0 + \alpha)$ OR $(Max - \alpha \leq Score(s_{jm}) \leq Max + \alpha)$
        create the rule: $rule_{s_{jm}}(c_i) \leftarrow s_{jm}$
        replace in $\mathcal{E}^+$, in $\mathcal{E}^-$ and in e, s_{jm} with $rule_{s_{jm}}(c_i)$
  while F (:= set of all leaf predicates of e) $\neq \emptyset$ **do**
    for all $l_i \in F$ **do**
      if l_i has only one parent (let $g_i(a_i, \ldots, a_n)$ be the l_i's parent) **then**
        create the rule: $rule_{l_i}(a_i, ...a_n) \leftarrow g_i, l_i$; H := true
        replace in $\mathcal{E}^+$, in $\mathcal{E}^-$ and in e, g_i, l_i with $rule_{l_i}(a_i, ...a_n))$
    for all $rule_i \leftarrow l_{i_1}, \ldots, l_{i_n}$ generated **do**
      if $\{l_{i_1}, \ldots, l_{i_n}\}$ occurs in some rule $rule_j$ **then**
        replace $l_{i_1}, \ldots, l_{i_n}$ in $rule_j$ by $rule_i$
        eliminate $rule_i$ form the set of rules generated
  Evaluate the set of generated rules

and $\mathcal{L}'$. The operational representation of function f is the Abstraction Theory that encoded the abstraction operators by means of a consistent set of clauses, i.e. domain rules (Definition 2). The proposed technique aims at learning such domain rules by looking for correspondences that often or seldom hold among a significant set of observations. These correspondences are generated according to the *inter-construction* operator (Definition 3) and are then exploited to simplify the description language in two different ways: by generating *shifting rules* that replace significant, characteristic or discriminant groups of literals by one single literal representing their conjunction, or by generating *neglecting rules* that eliminate groups of literals that are not significant. Both kinds of rules will be applied in order to perform the shift of language bias according to the absorption operator presented in Definition 3.

Algorithm 1 sketches the overall procedure conceived to discover common paths in the application domain that potentially could make up the Abstraction Theory. It firstly generates domain rules involving unary predicates only, that represents the characteristic of an object in the description, and then the rules made up of predicates whose arity is greater than 1, that represent the relationships between two or more object contained in the descriptions. Crucial point of the algorithm is the choice of the observation (referred to in the following as the *seed*) that will act as the representative of the concept that one would abstract. Currently it is the first encountered positive observation. Once the seed

is identified, for each constant c_i in its description, the algorithm finds all the unary predicates the constant is argument of. Among the identified subsets we discard those having cardinality equal to 0, that do not give information about the object, or 1, that provide only properties of the objects.

Each subset such identified is a potential candidate to compose the body of a rule, in the Abstraction Theory, made up of unary predicates. The selection among these subsets is done considering the ones that are the best representative for the class of the concept to be abstracted according to the seed e. Thus, each subset is assigned a score based on the number of times that it occurs in the positive and negative descriptions. This value represents the *coverage rate* of the subset with respect to the observations and indicates the quality of the subset. This kind of selection allows to choose the subsets that are neither too specific, because of they are present in few observations, nor too general, because of they are encountered in almost all the observations. Once the subsets s_j are selected, the rules to make the Abstraction Theory are formulated in the following way:

$$abstract\_predicate(c_i) \leftarrow s_j \quad \text{iff} \quad score(s_j) \geq P \qquad \text{(shifting rule)}$$
$$\leftarrow s_j \quad \text{iff} \quad score(s_j) \leq P \qquad \text{(neglecting rule)}$$

where P is a threshold depending on the application domain at handle[2]. In the first case, the rule's body, i.e. s_j that is a conjunction of literals, is present in almost all the observations thus it is fundamental for the learning process and thus the corresponding rule represents a shifting rule in the Abstraction Theory. In the second case the rule could indicate a detail in the description that is not very significant for the learning process and thus it is considered a neglecting rule. In both cases, replacing the rule's body with its head in the description of the observations reduces the length of observations, this way making the learning process more efficient.

The algorithm follows with the identification of rules made up of predicates whose arity is greater than 1 representing the relationships between two or more objects. Thus, once the abstraction rules, that are identified in the previous step, are replaced in all the observations, they don't contain any unary predicates belonging to the original representation language. At this point, an iteration that groups together the n-ary predicates is performed until one of the following conditions succeeds: 1) the description of the seed e does not contain *leaf predicates* (predicates that share arguments with at least an other predicate, excluding the head's predicate); 2) all the rules generated at step n have already been generated at step $n-1$.

The search of the leaf predicates is particularly complex due to the large number of relationships that could hold between the objects in the descriptions. The identification of such predicates is done by representing the observation with a tree (see Figure 1 for an example) in which each level is determined by the propagation of the variables/constants (no relation has to be imposed between two or more predicates at the same level even if they share some variable/constant): the root is the head of the observation and its direct descendants

[2] In order to make P independent on the specific domain, the score can be normalized as a percentage of the maximum score actually computed in the given dataset.

are all the predicates that share with it at least one argument. This procedure is iterated until all the predicates in the description have been inserted in the tree (a considered predicate does not participate anymore to the tree construction).

After the tree is constructed, we select the leaf nodes that have only one parent, let be $L = l_1, l_2, \ldots, l_n$ the set of such leaf predicates. Successively, for each element $l \in L$ its parent is extracted form the tree, let be it the literal $g(a_1, \ldots, a_m)$, and the following rule is generated:

$$rule(a_1, \ldots, a_m) \leftarrow g(a_1, \ldots, a_m), l$$

Finally, for each generated rule $rule_i \leftarrow l_{i_1}, \ldots, l_{i_n}$, if the body of $rule_i$, i.e. $l_{i_1}, \ldots, l_{i_n}$, appears in some rule $rule_j$ then $l_{i_1}, \ldots, l_{i_n}$ is replaced in $rule_j$ by the predicate $rule_i$ and the rule $rule_i$ is eliminated by the set of rules that are being generated. At the end of this step again the evaluation phase of the potential rules to make up the Abstraction Theory is performed according to the procedure above mentioned.

In order to associate a score to each subset we need a statistical model able to take into account the significance of the subset for the descriptions, i.e. its frequency in them. Specifically, a good subset is the one that has a great discriminating power, i.e. that is able to discriminate better than any other subset a description from the others. To this aim we exploit the distribution of the subset in the whole set of observations: an high discriminating power means that the subset is fundamental for the concept description since it helps to distinguish a concept from another, on the other hand a low discriminating power is interpreted as a hint that the subset is superfluous for the learning process and thus it could be eliminated from the description of the observations.

The statistical model that reflects such considerations is represented by the *Term Frequency - Inverse Document Frequency (TF-IDF)* [13] adapted to our work context facing with positive and negative observations. In the following a brief description of the method adapted to our context is provided.

For each subset S_i we create a vector $V_i = (V_{i1}, V_{i2}, \ldots, V_{iN})$ where N is the number of the available observations and V_{ij} is the weight of the i-th subset in the j-th observation that is computed as:

$$V_{ij} = FREQ_{ij} * (\lg \frac{N}{IFREQ_i} + 1)$$

The term $(\lg \frac{N}{IFREQ_i} + 1)$ represents the inverse of the frequency of the subset i in the whole set of observations. The result of this computation will be positive if the j-th observation is a positive observation, negative otherwise, thus the resulting vector will be of the form $V_i = (+, -, +, +, -, +, \ldots)$. This will allow to distinguish the significance of the subset according to its presence in the positive and negative observations.

Now, for each subset we have the vector of its weights in each observation. To select the best subset the following value is computed for each subset i:

$$score(s_i) = \sum_{j=1,\ldots,N} V_{ij}$$

It is worth noting that this score will be around zero if the subset equally occurs in both positive and negative observations, in which case it is considered insignificant and could be exploited as a neglecting rule in the abstraction phase. Conversely, an high absolute value indicates a strong correlation of the subset

with the positive or the negative observations. Specifically, highly positive (resp., negative) scores indicate that the subset is very frequent in the positive (resp., negative) observations. In both cases, it is considered significant and hence it could be exploited to build shifting rules for the abstraction phase.

Example 1. Let $h(1) : -p(1,2), p(1,4), p(1,5), c(2,3), f(5,6), d(4), s(6)$ the seed chosen in the set of the observations.

- **Step 1**:
  - *Grouping unary predicates:*
    $S = \emptyset$, no groups of unary predicates with cardinality strictly greater than 1 can be recognized;
- **Step 2**:
  - *Recognize Leaf Nodes:*
    $F = \{c(2,3),\ d(4),\ s(6)\}$, indeed $c(2,3)$ has only one parent $p(1,2)$; $d(4)$ has only one parent $p(1,4)$; $s(6)$ has only one parent $f(5,6)$.
  - *Create the rules - $rule_{l_i}(a_i, ...a_n) \leftarrow g_i, l_i$:*
    $c(2,3)$ with parent $p(1,2) \rightarrow rule1(X,Y) : -p(X,Y), c(Y,Z)$.
    $d(4)$ with parent $p(1,4) \rightarrow rule2(X,Y) : -p(X,Y), d(Y)$.
    $s(6)$ with parent $f(5,6) \rightarrow rule3(X,Y) : -f(X,Y), s(Y)$.
  - *Replace the rule in the set of the observations, for example:*
    $h(1) : -p(1,2), p(1,4), p(1,5), c(2,3), f(5,6), d(4), s(6). \rightarrow$
    $h(1) : -rule1(1,2), rule2(1,4), p(1,5), rule3(5,6)$.
- **Step 3**:
  - *Recognize Leaf Nodes:*
    $F = \{rule3(5,6)\}$, indeed $rule3(5,6)$ has only one parent $p(1,5)$.
  - *Create the rules - $rule_{l_i}(a_i, ...a_n) \leftarrow g_i, l_i$:*
    $rule3(5,6)$ with parent $p(1,5) \rightarrow rule4(X,Y) : -p(X,Y), rule3(Y,Z)$.
  - *Replace the rule in the set of the observations:*
    $h(1) : -rule1(1,2), rule2(1,4), p(1,5), rule3(5,6). \rightarrow$
    $h(1) : -rule1(1,2), rule2(1,4), rule4(5,6)$.
- **Step 4**: END - No more Leaf Nodes can be recognized

Figure 1 reports the steps 2 and 3 of the tree and rule construction. The procedure follows with the evaluation step of the generated rules, that are:
$rule1(X,Y) : -p(X,Y), c(Y,Z)$. $\quad rule2(X,Y) : -p(X,Y), d(Y)$.
$rule3(X,Y) : -f(X,Y), s(Y)$. $\quad rule4(X,Y) : -p(X,Y), rule3(Y,Z)$.
Now, suppose that P, the percentage empirically computed on the domain at handle, is equal to 95% and that the Score Percentage of each rule is: $score(1) = 95\%$; $score(2) = 99\%$; $score(3) = 75\%$; $score(4) = 86\%$. Then, $rule1$ and $rule2$ will be shifting rules while $rule3$ and $rule4$ neglecting rules:
$rule1(X,Y) : -p(X,Y), c(Y,Z)$. $\quad rule2(X,Y) : -p(X,Y), d(Y)$.
$: -f(X,Y), s(Y)$. $\quad : -p(X,Y), rule3(Y,Z)$.

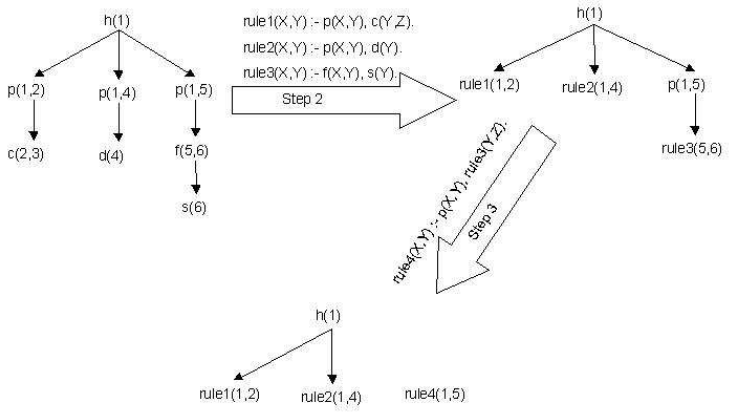


Fig. 1. Tree construction of an observation

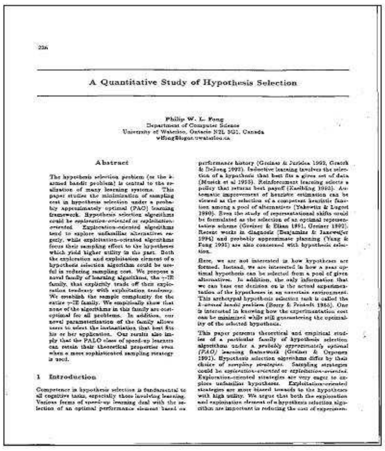
4 Experimental Results

The proposed method was implemented in SICStus Prolog and tested providing the resulting abstraction theories to the incremental ILP learning system INTHELEX [4] allowing it to exploit its multistrategy capabilities, in particular the abstraction one. Various experiments were carried out on a real world application domain of scientific paper documents [5].

The learning tasks to which the learning system was applied, involved the induction of classification rules for three classes of scientific papers (96 documents of which 28 for `ICML`, 32 for `SVLN`, 36 for `IEEET`), and of rules for identifying the logical components *Author* [36+, 332-], *Page Number* [27+, 341-] and *Title* [28+, 340-] in the `ICML` papers (in square brackets the number of positive and negative instances for each label are reported). Figure 2 shows an example of document and its *simplified*[3] description in first order language. 33 repetitions of each learning task were carried out, in each of which the dataset was randomly split into a training set (including 70% of the observations), exploited also to induce the rules for the abstraction operators) and a test set (made up of the remaining 30%).

To build neglecting rules, the threshold for considering low discriminating power (i.e. the score near to zero) was empirically set to $\pm 5\%$ of the minimum positive value and of the maximum of the negative ones in the vector associated to the rule. To build shifting rules that have an high discriminating power (i.e. very frequent in positive observations and rarely present in negative observations) the threshold was empirically set to the score less then 95% of the minimum positive value and of the maximum of the negative ones in the vector associated to the rule for the classification task and less then 75% of the

[3] In the figure we report an extract of the whole description that is made up of 112 literals on average


A Quantitative Study of Hypothesis Selection

Philip W. L. Fong

Abstract

1 Introduction

```
class_icml(icml_1) :-
    part_of(icml_1, icml_2),
    part_of(icml_1, icml_3),
    part_of(icml_1, icml_4),
    part_of(icml_1, icml_5),
    width_very_small(icml_2),
    width_very_large(icml_3),
    width_large(icml_4),
    width_very_large(icml_5),
    height_very_very_small(icml_2),
    height_smallest(icml_3),
    height_very_very_small(icml_4),
    height_smallest(icml_5),
    type_of_text(icml_2),
    type_of_hor_line(icml_3),
    type_of_text(icml_4),
    type_of_hor_line(icml_5),
    pos_right(icml_2),
    pos_center(icml_3),
    pos_center(icml_4),
    pos_center(icml_5),
    pos_upper(icml_2),
    pos_upper(icml_3),
    pos_upper(icml_4),
    pos_upper(icml_5),
    on_top(icml_3, icml_4),
    on_top(icml_3, icml_5),
    on_top(icml_4, icml_5),
    alignment_left_col(icml_3, icml_5),
    alignment_right_col(icml_3, icml_5),
    alignment_center_col(icml_3, icml_5).
```

Fig. 2. Sample ICML document and relative *simplified* description

minimum positive value and of the maximum of the negative ones in the vector associated to the rule for the understanding task.

The average results on the 33 folds, along with the number of refinements and of clauses learned, the predictive accuracy of the learned theories and the runtime (sec), are reported in Table 1. According to a paired t-test, there is no statistical difference between the results with and without abstraction, except for runtime. Having the same performance (predictive accuracy) and behavior (no. of clauses and refinements) both with and without abstraction means that the proposed technique was actually able to eliminate superfluous details only, leaving all the information that was necessary for the learning task, which was a fundamental requirement for abstraction. Conversely, runtime was dramatically reduced when using abstraction thanks to the shorter descriptions obtained by eliminating the details, which was exactly the objective of using abstraction.

An example of neglecting rule identified with the proposed strategy is:

```
:- type_graphic(A), pos_upper(A).
```

by which we understand that a graphics being placed in upper position is not discriminant between positive and negative examples. As expected, exploiting the abstraction operators the system learns shorter clauses. For instance, the theory learned for *author* contains two clauses made up of 18 and 15 literals (against the 19 and 37 without using abstraction):

```
logic_type_author(A) :- height_medium_small(A), pos_upper_type_text(A),
   part_of(B, A), part_of(B, C), height_very_small_type_text(C),
```

Table 1. System performance exploiting the discovered abstraction theories

	ICML		SVLN		IEEET	
	With Abs	No Abs	With Abs	No Abs	With Abs	No Abs
Lgg	5.81	5.54	7.36	8.12	8.03	8.30
Cl	1.21	1.27	2.75	2.69	2.03	2.27
Accuracy	96.93%	96.75%	86.54%	87.36%	90.69%	90.57%
Runtime	2.00	3.16	11.34	19.46	7.64	27.55

	Author		Page Number		Title	
ICML	With Abs	No Abs	With Abs	No Abs	With Abs	No Abs
Lgg	8.9	8.96	8.15	8.12	8.81	9.09
Cl	2.33	2.06	2.39	2.45	2.42	2.54
Accuracy	97.18%	97.12%	97.81%	97.54%	98.12%	97.87%
Runtime	14.44	29.07	34.06	76.22	27.70	51.67

```
   pos_upper_type_text(C), part_of(B, D), width_very_large(D),
   height_smallest(D), type_hor_line(D), pos_center_pos_upper(D),
   alignment_left_col(D, E), on_top(F, E), part_of(B, E), part_of(B, F),
   part_of(B, G), type_text_width_medium_large(G), pos_left_type_text(G).
logic_type_author(A) :- part_of(B, A), part_of(B, C),
   pos_upper_type_text(A), pos_center_pos_upper(A),
   pos_upper_type_text(C), pos_left_type_text(C),
   height_very_very_small_type_text(C), on_top(C, D),
   part_of(B, D), on_top(E, A), width_very_large(E), height_smallest(E),
   pos_center_pos_upper(E), on_top(F, E), alignment_center_col(F, E).
```

where the presence of several abstract predicates confirms that the automatically generated abstraction theory was able to identify discriminative intermediate concepts. An example of shifting rule learned (and exploited above) is:

```
pos_upper_type_text(A) :- type_text(A), pos_upper(A).
```

5 Conclusion and Future Works

The integration of inference strategies supporting pure induction in a relational learning setting, such as *abstraction* to reason at multiple levels, can be very advantageous both in effectiveness and efficiency for the learning process. In inductive learning, the shift to a higher level representation can be performed directly when the abstraction theory is given and usually an expert domain has to built such a theory. This paper presented a technique for automatically inferring meta-information needed to apply abstraction operators in an inductive learning framework, exploiting the same observations that are input to the inductive algorithm. Application of the proposed technique in a real learning system proved its viability for significantly improving learning time in complex real-world domains. Future work will concern the analysis of heuristics to choose the seed, to improve the generation of abstraction theories and the design of techniques that can provide information for further abstraction operators.

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